

MAT 170 Brief Calculus with Applications 3 credits

Description:

Provides an introduction to differential and integral calculus with applications in biological sciences, social sciences, physical sciences, or business with an analysis of algebraic, exponential, and logarithmic functions. (Students may not receive credit for both MAT 170 and MAT 175.)

Components: Lecture: 3 credit hours (45 contact hours).

Pre-requisites: Successful completion of MAT 150 or Math ACT 27 or above.

Implementation: Spring 2011

General Education: Mathematics

Competencies:

Upon completion of this course, the student can:

1. Approximate limits graphically and numerically and evaluate limits analytically.
2. List the conditions for the continuity of a function at a point and determine if a function is continuous or discontinuous at a point.
3. Determine the intervals of continuity of a function.
4. Evaluate infinite limits and limits at infinity.
5. Define the derivative of a function and evaluate the derivative of a function using the definition.
6. Evaluate the derivative of a function using differentiation rules for algebraic functions as well as product, quotient, and chain rules.
7. Use the derivative of a function to find the equation of the line tangent to the graph of the function at a given point.
8. Sketch the graph of a function using the first and second derivatives to determine the critical points, intervals on which the function is either increasing or decreasing, relative extrema, intervals on which the graph is either concave up or concave down, and inflection points of the graph.
9. Perform implicit differentiation.
10. Use derivatives to solve application problems including problems involving related rates and optimization for biological sciences, social sciences, physical sciences, or business.
11. Define the differential and use differentials to approximate function values.
12. Find indefinite and definite integrals of a function using integration rules for algebraic functions.
13. Find definite and indefinite integrals using substitution.
14. Find the average value of a function on an interval.
15. Use definite integrals to find the area under a curve and the area between two curves.
16. Determine if a function is differentiable or nondifferentiable at a point.
17. Find the derivative and integral of functions including polynomial, rational, root, exponential, and logarithmic functions.
18. Solve application problems using integrals for biological sciences, social sciences, physical sciences, or business.

Outline:

- I. Limits
 - A. Finding limits graphically
 - B. Approximating limits numerically
 - C. Finding limits analytically
 - D. One-sided limits
 - E. Continuity
 - F. Infinite limits ($f(x) \rightarrow \pm\infty$)
 - G. Limits as $x \rightarrow \pm\infty$
 - H. Horizontal asymptotes

- I. Vertical asymptotes
- II. Differentiation
 - A. Definition of the derivative
 - B. Finding derivatives using the definition
 - C. Finding the tangent line to the graph of a function
 - D. Basic differentiation rules for algebraic functions, product and quotient rules, chain rule
 - E. Finding the tangent line to a graph
 - F. Implicit Differentiation
- III. Applications of Differentiation
 - A. Related rate applications
 - B. Finding critical numbers
 - C. First derivative test/increasing/decreasing
 - D. Finding relative maxima and minima
 - E. Concavity and inflection points
 - F. Second derivative test
 - G. Curve sketching
 - H. Optimization applications
 - I. Differentials
- IV. Integration
 - A. Fundamental theorem of calculus
 - B. Finding the average value of a function
 - C. Properties of definite integrals
 - D. Integration using substitution
- V. Applications of Integration
 - A. Area under curve
 - B. Area between two curves

Learning Resources:

Berresford, G. & Rockett, A. (2004). *Brief applied calculus (3rd ed.)*. Boston, MA: Houghton/Mifflin

Lial, M. L., Greenwell, R. N., & Ritchey, N. P. (2005). *Calculus with applications, brief version (8th ed.)*. Boston, MA: Pearson/Addison Wesley.

Dates of Actions:

Approved: February 2006

Revised: April 2010